

1. Find the volume of the solid bounded in the first octant bounded by the cylinder $z = 9 - y^2$ and the planes $x = 1$.

2. Evaluate the double integral.

$$\iint_D x \cos y \, dA \quad \text{where } D \text{ is bounded by } y = x^2, y = 0 \text{ and } x = 3.$$

3. Use Stoke's theorem to evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$, $\mathbf{F}(x, y, z) = 6yx^2\mathbf{i} + 2x^3\mathbf{j} + 6xy\mathbf{k}$,

C is the curve of intersection of the hyperbolic paraboloid $z = y^2 - x^2$ and the cylinder $x^2 + y^2 = 25$ oriented counterclockwise as viewed from above.

4. The **flow lines** (or **streamlines**) of a vector field are the paths followed by a particle whose velocity field is the given vector field. Thus, the vectors in a vector field are tangent to the flow lines. The flow lines of the vector field $\mathbf{F}(x, y) = 6x\mathbf{i} - 12y\mathbf{j}$

satisfy the differential equations

$$\frac{dx}{dt} = 6x \quad \text{and} \quad \frac{dy}{dt} = -12y$$

Solve these differential equations to find the equations of the family of flow lines.

5. Find all the second partial derivatives of $f(x, y) = 2x^3y - 6xy^2$.
6. Use polar coordinates to find the limit.

$$\lim_{(x, y) \rightarrow (0, 0)} \frac{x^7 + y^7}{x^6 + y^6}$$